A Study of Global Inference Algorithms in Multi-Document Summarization

Ryan McDonald

Google Research 76 Ninth Avenue, New York, NY 10011 ryanmcd@google.com

Abstract. In this work we study the theoretical and empirical properties of various global inference algorithms for multi-document summarization. We start by defining a general framework and proving that inference in it is NP-hard. We then present three algorithms: The first is a greedy approximate method, the second a dynamic programming approach based on solutions to the knapsack problem, and the third is an exact algorithm that uses an Integer Linear Programming formulation of the problem. We empirically evaluate all three algorithms and show that, relative to the exact solution, the dynamic programming algorithm provides near optimal results with preferable scaling properties.

1 Introduction

Automatically producing summaries from large sources of text is one of the oldest studied problems in both IR and NLP [9, 17]. The expanding use of mobile devices and the proliferation of information across the electronic medium makes the need for such technology imperative. In this paper we study the specific problem of producing summarizes from clusters of related documents – commonly known as multi-document summarization. In particular, we examine a standard paradigm where summaries are built by extracting relevant textual units from the documents [6, 12, 15, 22].

When building summaries from multiple documents, systems generally attempt to optimize three properties,

- Relevance: Summaries should contain informative textual units that are relevant to the user.
- Redundancy: Summaries should not contain multiple textual units that convey the same information.
- Length: Summaries are bounded in length.

Optimizing all three properties jointly is a challenging task and is an example of a *global inference problem*. This is because the inclusion of relevant textual units relies not only on properties of the units themselves, but also properties of every other textual unit in the summary. Unlike single document summarization, redundancy is particularly important since it is likely that textual units from different documents will convey the same information. Forcing summaries to obey a length constraint is a common set-up in summarization as it allows for a fair empirical comparison between different possible

outputs [1, 16]. Furthermore, it represents an important "real world" scenario where summaries are generated in order to be displayed on small screens, such as mobile devices.

This global inference problem is typically solved in one of two ways. The first is to optimize relevance and redundancy separately. For example, the work of McKeown et al. [18] presents a two-stage system in which textual units are initially clustered, and then representative units are chosen from each cluster to be included into the final summary. Here, the clustering stage minimizes redundancy and the representative unit selection maximizes relevance. The second approach is to treat the problem truly as one of global inference and optimize all criteria in tandem. Goldstein et al. [12] presented one of the first global models through the use of the maximum marginal relevance (MMR) criteria, which scores sentences under consideration as a weighted combination of relevance plus redundancy with sentences already in the summary. Summaries are then created with an approximate greedy procedure that incrementally includes the sentence that maximizes this criteria. Currently, greedy MMR style algorithms are the standard in summarization [6].

More recently, Filatova and Hatzivassiloglou [10] described a novel global model for their event-based summarization framework and showed that inference within it is equivalent to a known NP-hard problem. Fortunately this led to availability of approximate greedy algorithms with proven theoretical guarantees. Daumé et al. [7] formulate the summarization problem in the structured prediction setting and present a new learning algorithm that sets model parameters relative to an approximate global inference algorithm. This method is advantageous since it easily allows for the incorporation of compression decisions as well. However, it assumes the existence of a training corpus.

In this work we study the theoretical and empirical properties of a variety of global inference algorithms for multi-document summarization. We start by defining a general framework and proving that inference in it is NP-hard. We then present and briefly analyze three inference algorithms. The first is a greedy approximate method that is similar in nature to the MMR algorithm of Goldstein et al. [12]. The second algorithm is an approximate dynamic programming approach based on solutions to the knapsack problem. The third algorithm provides an exact solution to the global inference problem using an Integer Linear Programming (ILP) formulation. This is feasible due to well known efficient branch-and-bound algorithms for solving large-scale ILPs. We empirically evaluate all three algorithms and show that, relative to the exact solution, the dynamic programming algorithm provides near optimal results with preferable scaling properties.

It is worth noting that the properties of global inference algorithms have been examined in related fields. Most similar to the current study is the work of Germann et al. [11]. In that work a number of machine translation inference algorithms were evaluated in terms of translation quality and CPU usage.

2 Global Inference

As input we are given a document collection $D = \{D_1, \ldots, D_k\}$. Each document D contains a set of textual units $D = \{t_1, \ldots, t_m\}$, which can be words, sentences,

paragraphs, etc. For simplicity, we represent the document collection simply as the set of all textual units from all the documents in the collection, i.e., $D = \{t_1, \ldots, t_n\}$ where $t_i \in D$ iff $\exists t_i \in D_j \in D$. We let $S \subseteq D$ be the set of textual units constituting a summary.

We define two primary scoring functions,

- 1. Rel(i): The relevance of textual unit t_i participating in the summary.
- 2. Red(i, j): The redundancy between textual units t_i and t_j . Higher values correspond to higher overlap in content.

These scoring functions are completely arbitrary and should be defined by domain experts. For instance, scores can include a term to indicate similarity to a specific query for query-focused summarization or include terms involving entities, coherence, domain specific features, etc. Scores can also be set by supervised learning algorithms when training data is available [22].

Finally, we will define the function l(i) to indicate the length of textual unit t_i . Length is also arbitrary and can represent characters, words, phrases, etc. As in most summarization studies, we assume that as input an integer K, for which the length of any valid summary cannot exceed.

Formally we can write the multi-document summarization inference problem as follows:

$$S = \underset{S \subseteq D}{\operatorname{arg\,max}} s(S) \tag{1}$$

$$= \underset{S \subseteq D}{\operatorname{arg\,max}} \sum_{t_i \in S} \operatorname{Rel}(i) - \sum_{t_i, t_j \in S, \ i < j} \operatorname{Red}(i, j)$$
such that $\sum_{t_i \in S} l(i) \le K$

We refer to s(S) as the *score* of summary S. We assume that redundancy scores are symmetric and the summation of scores is over i < j to prevent counting redundancies multiple times. If desired, we could unevenly weight the relevance and redundancy scores to prefer one at the expense of the other. It is also worth mentioning that the redundancy factors in Equation 1 are pairwise. This is a slight deviation from many systems, in which the redundancy of unit t_i is calculated considering the rest of the summary in its entirety. For now, we have simplified the redundancy factor to a sum of pairwise relationships because it will allow us to define an Integer Linear Programming formulation in Section 2.2. In turn, this will allow us to compare our approximate algorithms to an upper bound in performance. In Section 3.4 we discuss alternate formulations to Equation 1.

The formulation presented in Equation 1 is very similar to the *classification with pairwise similarities* problem studied by Kleinberg and Tardos [14]. There are also strong connections to work in Markov random fields as well as information extraction [21]. One of the primary differences here is the addition of a length constraint. This formulation also does not specify any ordering preferences on the textual units extracted for the summary [2]. Such constraints can help make a summary more coherent for the user. It is possible to determine order as a post-processing stage, but an interesting extension of this work would be to incorporate them directly into inference.

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2.1 Global Inference is NP-hard

For completeness we prove here that inference in a global summarization system is NP-hard through a reduction from 3-D matching (3DM).

3DM: Disjoint sets X, Y, Z each with m distinct elements and a set $T \subseteq X \times Y \times Z$. Question: is there a subset $S \subseteq T$ such that |S| = m and each $v \in X \cup Y \cup Z$ occurs in exactly one element of S?

Reduction: $\forall a = (x, y, z) \in T$, set Rel(a) = 1, otherwise Rel(a) = 0. Furthermore, $\forall a = (x, y, z), a' = (x', y', z') \in T$ set Red(a, a') = 0 iff $x \neq x'$ and $y \neq y'$ and $z \neq z'$, otherwise $s(a, a') = \infty$. Finally, set l(a) = 1 and K = m

Theorem: There is a 3D matching iff the highest scoring summary has a score of exactly K. **Proof**: First we observe that if there is a 3DM then the highest scoring summary will have a score of K. Clearly no summary could have a score greater than K (due to the length constraint). Furthermore, if we let the summary consist of just the tuples from the 3DM, the the score will be exactly K since each tuple contributes 1 to the overall score and there are no $-\infty$ pairwise factors. Next we observe that if there is a summary of score K, then there must be 3DM. This is easily seen by examining the tuples returned in the summary. There must be m of them (since K = m). Furthermore, none of the tuples can overlap, otherwise a pairwise $-\infty$ score would have been added to the overall score.

Therefore if we could solve the global inference problem tractably, we could answer the 3DM problem in polynomial time. It is not difficult to show that the major source of intractability are the redundancy terms from Equation 1. In fact, it is possible to re-write the reduction *only* in term of redundancy scores (i.e., if $\sum_i Rel(i) = 0$ and $K = \infty$). When the redundancy terms are removed (i.e., $\sum_{ij} Red(i, j) = 0$), the problem is still NP-hard and can be shown to be equivalent to the 0-1 knapsack problem [5]. There does exist a O(Kn) algorithm for solving the knapsack problem, but this only makes it pseudo-polynomial, since K is represented as log K bits in the input. However, for the summarization problem K is typically on the order of hundreds, making such solutions feasible. We will exploit this fact in Section 2.2.

2.2 Global Inference Algorithms

Greedy Algorithm. A simple approximate procedure to optimizing Equation 1 is to begin by including highly relevant textual units, and then to iteratively add new units that maximize the objective. This algorithms is outlined in Figure 1a and is a variant of MMR style algorithms. The advantage of this algorithm is that it is simple and computationally efficient. The runtime of this algorithm is in the worst case $O(n \log n + Kn)$ due to the sorting of n items and because each iteration of the loop takes O(n) and the loop will iterate at most K times. This assumes the unlikely scenario when all sentences have a length of one. In practice, the loop only iterates a small number of times. We also assume that calculating s(S) is O(1) when it is really a function of loop iterations, which again makes it negligible.

It is not difficult to produce examples for which this greedy procedure will fail. In particular, the choice of including the most relevant sentence in the summary (Figure 1a, line 2) can cause error propagation. Consider the case of a very long and highly relevant

(b) Knapsack Algorithm				
1. $S[i][0] = \{\} \forall 1 \le i \le n$				
2. for $i: 1 n$				
3. for $k: 1 K$				
4. $S' = S[i-1][k]$				
5. $S'' = S[i-1][k-l(i)] \cup \{t_i\}$				
6. if $s(S') > s(S'')$ then				
7. $S[i][k] = S'$				
8. else				
9. $S[i][k] = S''$				
10. return $\arg \max_{S[n][k], k \leq K} s(S[n][k])$				

Fig. 1. (a) A greedy approximate algorithm. (b) A dynamic programming algorithm based on solutions to the knapsack problem.

sentence. This sentence may contain a lot of relevant information, but it may also contain a lot of noise. Including this sentence in the summary will help maximize relevance at the cost of limiting the amount of remaining space for other sentences. This scenario does in fact happen frequently when summarizing news, where sentence length is typically very long. Ideally, we would prefer a shorter sentence – possibly from another document – that contains similar information, but is more compact.

Dynamic Programming Algorithm. To alleviate this problem we devise a dynamic programming solution. Recall that the input to the problem is a set of textual units, $D = \{t_1, \ldots, t_n\}$, and an integer K. Let S[i][k], where $i \leq n$ and $k \leq K$, be a high scoring summary of exactly length k that can only contain textual units in the set $\{t_1, \ldots, t_i\}$. Figure 1b provides an algorithm for filling in this table. This algorithm is based on a solution to the 0-1 knapsack problem [5]. In that problem the goal is to fill a knapsack of capacity K with a set of items, each having a certain weight and value. The optimal solution maximizes the overall value of selected items without the total weight of these items exceeding K. Clearly if one could ignore the redundancy terms in Equation 1, the summarization problem and knapsack problem would be equivalent, i.e., value equals relevance and weight equals length. Of course, redundancy terms are critical when constructing summaries and we cannot ignore them.

The crux of the algorithm is in lines 4-10. To populate S[i][k] of the table, we consider two possible summaries. The first is S[i-1][k], which is a high scoring summary of length k using textual units $\{t_1, \ldots, t_{i-1}\}$. The second is a high scoring summary of length k - l(i) plus the current unit t_i . S[i][k] is then set to which ever one has highest score. The knapsack problem is structured so that the principle of optimality holds. That is, if for i' < i and $k' \leq k$, if S[i'][k'] stores the optimal solution, then S[i][k] will also store the optimal solution. However, the additional redundancy factors in the multi-document summarization problem, which are included in the score calculations of line 6, break this principle making this solution only approximate for our purposes. The final line of the algorithm simply looks for the highest scoring summary within the length bound and returns it.

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The advantage of using a knapsack style algorithm is that it eliminates the errors caused by the greedy algorithm inserting longer sentences and limiting the space for future inclusions. Consider the trivial example with three items, A, B, and C, where Rel(A) = 3, Rel(B) = 2, Rel(C) = 2, l(A) = 4, l(B) = 3, l(C) = 2, K = 5, and all redundancy factors are 0. The greedy algorithms will include just A, but the knapsack algorithm will return the optimal solution of B and C.

The runtime of this algorithm is $O(n \log n + Kn)$ if we again assume that $s(S) \in O(1)$. However, this time K is not a worst-case scenario, but a fixed lower-bound on runtime. Even so, most summarization systems typically set K on the order of 100 to 500, making such solution easily computable (see Section 3). Note also that the correctness of the algorithm as given in Figure 1 is based on the assumption that there is a valid summary of every length $k \leq K$. It is not difficult to modify the algorithm and remove this assumption by checking that both S' and S'' truly have a length of k.

One additional augmentation that can be made to both the greedy and knapsack algorithms is the inclusion of a beam during inference. This was implemented but found to have little impact on performance unless a beam of substantial size was used, which resulted in a increase in run-time.

ILP Formulation. It would be desirable to compare the previous two algorithms with an exact solution to determine how much accuracy is lost due to approximations. Fortunately there is a method to do this in our framework through the use of Integer Linear Programming (ILP). ILP techniques have been used in the past to solve many intractable inference problems in both IR and NLP. This includes applications to relation and entity classification [21], sentence compression [4], temporal link analysis [3], as well as syntactic and semantic parsing [19, 20].

An ILP is a constrained optimization problem, where both the cost function and constraints are linear in a set of integer variables. Solving arbitrary ILPs is an NP-hard problem. However, ILPs are a well studied optimization problem with efficient branch and bound algorithms for finding the optimal solution. Modern commercial ILP solvers can typically solve moderately large optimizations in a matter of seconds. We use the GNU Linear Programming kit¹, which is a free optimization package.

The multi-document global inference problem can be formulated as the ILP in Figure 2. In this formulation we include indicator variables α_i and α_{ij} , which are 1 when a textual unit or pairs of textual units are included in a summary. The goal of the ILP is to set these indicator variables to maximize the payoff subject to a set of constraints that guarantee the validity of the solution. The first constraint simply states that the indicator variables are binary. The second constraint states that for all sentences included in the summary, the sum of their lengths must be less than our predefined maximum. Constraints (3) to (5) ensure a valid solution. Constraints (3) and (4) simply state that if the summary includes both the units t_i and t_j then we have to include them individually as well. Constraint (5) is the inverse of (3) and (4).

¹ http://www.gnu.org/software/glpk/

maximize $\sum_{i} \alpha_i \operatorname{Rel}(i) - \sum_{i < j} \alpha_{ij} \operatorname{Red}(i, j)$

such that $\forall i, j$: (1) $\alpha_i, \alpha_{ij} \in \{0, 1\}$ (4) $\alpha_{ij} - \alpha_j \leq 0$ (2) $\sum_i \alpha_i l(i) \leq K$ (5) $\alpha_i + \alpha_j - \alpha_{ij} \leq 1$ (3) $\alpha_{ij} - \alpha_i \leq 0$

Fig. 2. ILP formulation of global inference.

2.3 Implementation Details

When implementing each algorithm it is important for the scale of the score functions to be comparable. Otherwise, the algorithms will naturally favor either relevancy or redundancy. Furthermore, there are quadratically many redundancy factors in a summary score compared to relevance factors. Depending on the scoring functions this can lead to summaries with a small number of very long sentences or a lot of very short sentences. One way to avoid this is to add new constraints specifying a desired range for sentence lengths. Alternatively, we found that replacing every score with its z-score alleviated many of these problems since that guaranteed both positive and negative values. When scores are predominantly negative, then the algorithms return summaries much shorter than K. This is simply fixed by changing the constraints to force summary lengths to be between K-c and K, where c is some reasonably sized constant.

In the ILP formulation, the number of constraints is quadratic in the total number of textual units. Furthermore, the coefficient matrix of this problem is not unimodular [21]. As a result, the ILP algorithm does not scale well (see Section 3 for more on this). To alleviate this problem, each algorithm passed through a preprocessing stage that sorted all textual units by relevance. Every textual unit not in the top 100 was discarded as unlikely to be in the final summary. In this way, all algorithms ran under the same conditions.

3 Experiments

In this study we used sentences as textual units. Each textual unit, document and document collection is represented as a bag-of-words vector with tf^*idf values. Length bounds are always in terms of words. In addition to the three algorithms described in this paper, we also ran a very simple baseline that is identical to the greedy algorithm, but does not include redundancy when scoring summaries.

We ran two primary sets of experiments, the first is on generic summarization and the second query-focused summarization. Results are reported using the ROUGE evaluation package [16]. ROUGE is a n-gram recall metric for an automated summary relative to a set of valid reference summaries. We report ROUGE-1 and ROUGE-2 scores, which capture unigram and bigram recall. We set the ROUGE evaluation package to use stemming and hard length bounds.

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(a)								
()		Summary Length		(b)		Original	Alternate	
		50	100	200			Oligiliai	Alternate
		26672	100	200		Baseline	34.4 / 5.4	34.4 / 5.4
	Baseline	26.6/5.3	33.076.8	39.4/9.6		Greedy	350/57	356/61
	Greedy	26.8 / 5.1	33.5/6.9	40.1 / 9.5		Uncertain 1	25.07.5.7	26.5.16.7
	Knansack	270/50	318173	41 2 / 10 0		Knapsack	35.776.2	36.5/6./
	Knapsack	21.91 3.9	54.877.5	41.27 10.0		ILP	35.8/6.1	N/A
	ILP	28.1/5.8	34.6/7.2	41.5 / 10.3				

Table 1. (a) Results for generic summarization experiments using DUC 2002 data set. Each cell contains the ROUGE-1 and 2 scores (R1 / R2). (b) Results for query-focused summarization experiments using DUC 2005 data set. *Original*: Using original inference formulation from Equation 1. *Alternate*: Using alternate inference formulation from Section 3.4.

3.1 Generic Experiments

In this general setting, a system is given a document collection D, and length bound K, and is asked to produce a summary that is most representative of the entire document collection. For these experiments, we used the DUC 2002 data set [13]. This data set contained 59 document collections, each having at least one manually created summary for lengths 50, 100, 200. We define the score functions as follows:

 $Rel(i) = POS(t_i, D)^{-1} + SIM(t_i, D)$ (where $t_i \in D$ and $D \in D$) $Red(i, j) = SIM(t_i, t_j)$

where POS(t, D) is the position of textual unit t in document D and SIM(a, b) is the cosine similarity between two vectors. Relevance scores prefer sentences that are near the beginning of documents and are maximally informative about the entire document collection. Again, these score functions are general and we only use these particular scoring criteria for simplicity and because we evaluate our approach on news stories².

Results are shown in Table 1a. The first thing to note is that incorporating redundancy information does improve scores, verifying previous work [10, 12]. Next, we see that scores for the sub-optimal knapsack algorithm are very near scores for the exact ILP algorithm and are even sometimes slightly better. This is due to the fact that redundancy scores are highly influential in the ILP solution. Highly relevant, but semantically different, sentences will often contain identical terms (i.e., person names or places). These sentences are then forced to compete with one another when constructing the summary, when it may be desirable to include them both. The final point we will make is that the greedy algorithms performance is consistently lower than the knapsack algorithm. An analysis of the resulting summaries suggests that indeed long sentences are getting included early, making it difficult to add relevant sentences later in the procedure.

² Preferring sentences near the beginning of documents is a typical requirement for summarizing news.



Fig. 3. Plots average number of seconds to summarize a document collection as a function of the number of textual units considered.

3.2 Query-focused Experiments

The query-focused setting requires summaries to be relevant to a particular query that has been supplied by the user. For these experiments, we used the DUC 2005 data sets [6]. This data consists of 50 document collections, each with a corresponding query. For each collection and query, multiple manually constructed summaries of 250 words were provided. The redundancy score of the system remained unchanged from the previous experiment. However, for a document collection D and query Q, the relevance score was changed to the following:

$$Rel(i) = SIM(t_i, Q) + SIM(t_i, D)$$

Thus, relevance is an equally weighted combination of similarity to the query and similarity to the entire document collection. Results are shown in Table 1b under the column *Original*. Again we see that the knapsack algorithm outperforms the greedy algorithm and has a score comparable to the ILP system.

3.3 Scaling Experiments

For the experiments just presented, inference was always only over data sets with less than 100 document collections, each with less than 100 documents, each document with 10 to 50 sentences. In practice, these algorithms should handle much larger data sets in order to be applied to real world problems such as summarizing search results. To test inference scalability, we restricted the number of textual units under consideration for a summary to 20, 50, 100 and 500, then measured the CPU time for each algorithm. Results are shown in Figure 3. This figure plots average number of seconds to summarize a document collection as a function of the number of textual units under consideration.

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It is clear that the ILP solution is feasible for small problems, but scales superlinearly making it an unlikely solution for larger tasks. On the other hand, both the greedy and knapsack solutions scale linearly with the size of the problem, which is not surprising given their runtime analysis. In fact, the greedy algorithms runtime is nearly constant, since overhead from preprocessing steps accounts for most of the CPU time.

3.4 Alternate Formulations

The global inference formulation given in Equation 1 has two primary motivations. The first is that it is a reasonably intuitive objective function. The second is that it allowed for an exact ILP formulation, which was necessary to test the approximate algorithms relative to an exact solution. One advantage of the approximate algorithms is that they can work with any definition of the score of a summary. For example, in query-focused summarization we might prefer the following:

$$s(S) = SIM(S, Q) + SIM(S, D)$$

Here the score of a summary is just the similarity of the summary to the query plus the similarity to the entire document collection. This looks similar to using Equation 1 under the definition of relevance from Section 3.2. However, now relevance is measured as the similarity of the entire summary to the query and document collection, instead of just the sum over each unit. There are also no explicit redundancy terms, as redundancy is managed by the similarity of the summary to the document collection (i.e., highly redundant summaries will match less content of the entire collection). As a result, this formulation is much simpler and concerns over scaling relevance and redundancy scores are non-existent. An ILP solution to this particular formulation is not possible since scores do not naturally factorize by textual units.

Results for the query-focused experiments are presented in Table 1b under the column *Alternate*. These results display an additional advantage of the knapsack algorithm over greedy and ILP solutions. Note that the performance of the baseline does not change, since this algorithm still uses the original definition of sentence relevance in isolation when producing summaries.

Other scoring functions are of possible. However, we found that most did not improve upon our original formulation from Equation 1.

4 Conclusions

In this work we studied three algorithms for global inference in multi-document summarization. We found that a dynamic programming algorithm based on solutions to the knapsack problem provided optimal accuracy and scaling properties, relative to both a greedy algorithm and an exact algorithm that uses Integer Linear Programming. Additionally, the greedy and knapsack algorithms are compatible with arbitrary scoring functions, which can benefit performance.

We have already begun to extend the algorithms presented here to jointly extract and compress sentences for summary inclusion using a sentence compressor similar to the one described by Dorr et al. [8]. Early results are promising and show that compression decisions are greatly improved with the knowledge of other sentences in the summary.

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